Unravelling parameter interactions in calcium alginate/polyacrylamide double network hydrogels using a design of experiments approach for the optimization of mechanical properties†

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Calcium alginate/polyacrylamide double network hydrogels were reported to be exceptionally tough. However, literature reports so far varied the sample compositions mainly by one parameter at a time approaches, thus only drawing an incomplete picture of achievable material properties. In this contribution, sample compositions are varied according to a face-centered central composite experimental design taking into account the four parameters of alginate concentration $c_{\text{Alg}}$, high/low molar mass alginate mixing ratio $R_{\text{p}}$, acrylamide concentration $c_{\text{AAm}}$, and $N,N'$-methylenebisacrylamide concentration $c_{\text{MBA}}$. Each sample composition is investigated in triplicate. Thus, 75 samples were investigated by tensile testing, and a detailed analysis of the significant parameters and parameter interactions influencing the mechanical properties is conducted. The data shows that two parameter interactions, involving all four tested parameters, have a large effect on the Young's modulus, the strength, the toughness and the strain at material failure. As a consequence, it becomes evident that the experimental procedure from previous studies did not always result in optimum sample compositions. The results allow optimization of the mechanical properties within the studied parameter space, and a new maximum value of the strength of 710 kPa is reported. The data also give rise to the assumption that other parameters and parameter interactions ignored in this study may allow further tailoring of mechanical properties.

Introduction

Hydrogels are highly attractive materials in such diverse fields such as tissue engineering, soft robotics, drug delivery, or sensing. This is facilitated by the many advantageous properties of hydrogels like biocompatibility, responsiveness, or permeability for solutes. However, one of the outstanding weaknesses of many hydrogel materials is their poor mechanical stability. Hydrogels typically have rather low Young’s moduli in the order of 10 kPa and rarely above 100 kPa, and fracture energies often below 10 J m$^{-2}$, limiting their application in load-bearing environments. One approach to overcome these shortcomings are the so-called double network (DN) hydrogels, consisting of two intertwined, independent, swollen polymer networks.

One popular DN hydrogel class is composed of chemically cross-linked polyacrylamide (PAAm) as the first network and physically cross-linked alginate (Alg) as the second network, first described by Sun et al. The Alg is most frequently cross-linked with Ca$^{2+}$ ions and the resulting materials are called Ca-Alg/PAAm DN hydrogels. When deforming these materials, crack bridging occurs by the PAAm network simultaneous to energy dissipation by unzipping ionic cross-links in the alginate network. As a result, Ca-Alg/PAAm DN hydrogels were shown to have outstanding properties, such as tunable Young’s moduli $E$ between just a few kPa up to approx. 1 MPa, and fracture energies of up to approx. 16 kJ m$^{-2}$. Among others, these remarkable characteristics have lead to applications of Ca-Alg/PAAm DN hydrogels in 3D printing, tissue engineering, stretchable optical fibers and electronics, wet adhesives, hydrogel folding, sensors, and actuators.

The exact material properties depend on the preparation conditions and the sample composition. Ca-Alg/PAAm DN hydrogel preparation is usually achieved by first forming the
PAAm network by free radical polymerization in the presence of sodium alginate (Na-Alg), followed by cross-linking of the Alg with Ca\(^{2+}\) ions (Scheme 1). In this context, especially the method to introduce the Ca\(^{2+}\) ions into the hydrogels was studied. Initial reports used CaSO\(_4\) particles dispersed in the precursor solution which slowly released Ca\(^{2+}\) ions into the formulation.\(^{24,39}\) However, due to limited solubility of CaSO\(_4\) the achieved cross-link density of Alg was low, so not the entire possible spectrum of mechanical properties was harnessed, and for examples the achieved Young’s moduli were relatively low up to approx. 300 kPa.\(^{24}\) Later, instead of using CaSO\(_4\) particles, the pre-formed PAAm hydrogel containing Na-Alg was submerged in rather concentrated CaCl\(_2\) solutions, allowing the Ca\(^{2+}\) ions to diffuse into the gel.\(^{25,26,29,40–42}\) The resulting high cross-link density of Alg allows the above mentioned high Young’s moduli up to 1000 kPa and fracture energies of up to 16 kJ m\(^{-2}\), albeit not for the same sample composition, if simultaneously the Alg concentration is adjusted accordingly.\(^{25}\) Another method involves a mixture of CaCO\(_3\) particles and \(\delta\)-lactone (GDL).\(^{43–45}\) GDL hydrolyzes slowly, thus lowering the pH and decomposing the CaCO\(_3\) to make the Ca\(^{2+}\) ions accessible in solution.

The description of the sample preparation process demonstrates that a multitude of parameters influence the final properties of the materials. Within the precursor solution, various components are present: The monomer acrylamide (AAm), the cross-linker \(\text{N} N’\text{-methylenediacrylamide (MBA)},\) a radical initiator (typically ammonium persulfate, APS), \(\text{N} N’,\text{N}’\text{-tetramethyl ethylenediamine as a catalyst, and Na-Alg.}\) The Na-Alg can come from different sources with varying molar mass or molecular structure.\(^{46}\) Finally, the concentration and application method of the calcium ion cross-linker is crucial.

The sample composition is governed by the concentrations of all components in the precursor solution. It becomes evident that it is difficult to study the whole parameter space for sample preparation, and thus it is difficult to access the optimum conditions, e.g., to maximize the Young’s modulus.

As a result, the pioneering studies published so far put forward mainly variations of one parameter at a time and thus provided a starting point to understand the Ca-Alg/PAAm DN hydrogel behavior. Sun \textit{et al.} varied the AAm fraction in the total monomer content \((c_{\text{AAm}} + c_{\text{Alg}})\) as well as changed the CaSO\(_4\) and MBA concentrations.\(^{24}\) Others studied different total Alg concentrations in the precursor solutions,\(^{25,26,41}\) or varied the APS concentration,\(^{33}\) MBA concentration,\(^{39}\) or used different metal ions to cross-link the Alg.\(^{35,40,47}\) Naficy \textit{et al.}\ and Fitzgerald \textit{et al.} in principle varied two parameters simultaneously (Alg/MAA MBA concentrations and MBA/Ca\(^{2+}\) cross-linker concentrations, respectively), however did not go into detail concerning possible parameter interactions.\(^{41,43}\) In order to illustrate what a two-factor interaction is, the data reported by Li \textit{et al.}\ is helpful.\(^{25}\) They showed an increase of \(E\) with increasing Alg concentration while keeping the AAm concentration constant. A change of the AAm concentration could of course have an effect on \(E\), but this is not the important point for a two-factor interaction. A two-factor interaction would mean that the change of AAm concentration, on top of its own effect, induces an additional change of the dependence of \(E\) with the Alg concentration, possibly causing a large leveraging effect on \(E\). Thus, such two-factor interactions can be expected to be extremely important for optimization of mechanical properties of Ca-Alg/PAAm hydrogels.

However, up to now no studies exist which cover a larger part of the parameter space concerning the sample composition, and as a consequence it is completely unknown in how far parameter interactions influence the outcome of the experiments and induce leveraging effects on the material properties. Therefore, we hypothesize that the ideal preparation conditions for Ca-Alg/PAAm DN hydrogels have not been found yet. In this contribution, we aim to systematically vary the following four important parameters dealing with the composition of the hydrogel precursor solution (Scheme 1) in a design of experiments (DoE) approach,\(^{48}\) and investigate their impact on the mechanical properties: (1) Alg concentration \(c_{\text{Alg}}\), (2) fraction \(R_p\), of high molar mass Alg in total Alg concentration, (3) AAm concentration, \(c_{\text{AAm}}\), (4) AAm concentration, \(c_{\text{AAm}}\),...
concentration $c_{\text{AAM}}$, and (4) MBA concentration $c_{\text{MBA}}$. We especially will study two parameter interactions in detail for the first time. We thus hope to contribute to a more comprehensive understanding of the principles that govern the Ca-Alg/PAAm DN hydrogel properties.

**Experimental**

**Materials**

The following materials were purchased from Sigma-Aldrich (Germany): Acrylamide (AAm, $\geq 99\%$), ammonium peroxodisulfate (APS, $\geq 98\%$), calcium chloride dihydrate (CaCl$_2$·2H$_2$O, $\geq 99\%$), disodium hydrogen phosphate (Na$_2$HPO$_4$, $\geq 99\%$), N,N,N',N'-methylenebisacrylamide (MBA, $99\%$), N,N,N',N'-tetramethyl ethylenediamine (TEMED, $99\%$). The sodium alginates Protanal LF 10/60 and Manucol LD were obtained from FMC BioPolymer (USA). Poly(methacrylic acid) (PMAA) standards were purchased from PSS Polymer Standards Service (Germany).

**Size exclusion chromatography**

The molar mass distribution of the two alginates Protanal LF 10/60 and Manucol LD were investigated at 40 °C by size exclusion chromatography using a 1260 infinity GPC-SEC analysis system (Agilent Technologies, USA) equipped with a Suprema Linear M column (PSS Polymer Standards Service, Germany) in the range of 1 kDa to 1000 kDa. A 0.07 M solution of Na$_2$HPO$_4$ in ultrapure water was used as the eluent and to dissolve the respective alginates (1 mg mL$^{-1}$). The flow rate was set to 1 mL min$^{-1}$, the injection volume was 50 μL. For universal calibration of the measuring system polymethacrylic acid standards were dissolved and measured with a concentration of 1 mg mL$^{-1}$ in Na$_2$HPO$_4$ (0.07 M) combining refractive index (RI) and viscometer detectors.

**General procedure for preparation of hydrogel samples for tensile tests**

Ca-Alg/PAAm DN hydrogels were prepared according to the experimental plan described below using a two-step method in which first the PAAm network is produced in the presence of sodium alginate (Scheme 1). For this purpose, the sodium alginate Protanal LF 10/60 and Manucol LD were mixed at the required concentrations with ultrapure water (30 mL) and stirred at 40 °C for 30 min. Subsequently, the mixture was agitated on a roller mixer at room temperature until the alginates were fully dissolved (typically approx. 1 h). Then AAm, MBA as well as APS were added in the required amounts and dissolved on the roller mixer for 15 min at room temperature. The solution was degassed in an ultrasonic bath at 40 °C for 15 min. This was followed by the addition of TEMED, which was dissolved using a roller mixer for one minute. The entire solution was pipetted into a mold consisting of two quartz glass panes separated by a silicone spacer (2 mm height) greased with polytetrafluoroethylene (PTFE) paste for better adhesion. Cross-linking of the PAAm network was carried out for 48 h at room temperature. After that, the gel was transferred into a Petri dish and covered entirely with 100 mL of a 0.5 M CaCl$_2$ solution. The sample was swollen for 48 h at room temperature, replacing the entire volume of the CaCl$_2$ solution after 24 h. After the swelling process, specimens for tensile tests in the shape of the S3A sample (DIN 53504: 2017-03) (Fig. S1, ESI†) were punched out of the DN hydrogels and examined.

**Experimental plan for the variation of the hydrogel composition**

Preparation parameters varied according to a DoE were the total alginate concentration $c_{\text{alg}}$, the fraction $R_D$ of the Protanal LF 10/60 concentration of the total alginate concentration, the concentration $c_{\text{AAM}}$ of AAm, and the concentration $c_{\text{MBA}}$ of MBA. The concentrations of the initiator APS and the catalyst TEMED were fixed relative to $c_{\text{AAM}}$ and were 0.42% and 0.25% of $c_{\text{AAM}}$ respectively. The ranges of the parameter values are given in Table 1.

In this study, parameter values were varied according to a face-centered central composite design, resulting in 25 different sample compositions (Table S2, ESI†). Each sample composition was prepared in triplicate, so that in total 75 independently prepared samples were investigated for their mechanical properties in a randomized order (Table S3, ESI†). For the mechanical tests, five samples were punched from each of the 75 samples and characterized in a tensile test.

**Uniaxial tensile tests**

The mechanical characterization of the Ca-Alg/PAAm DN hydrogels was carried out by uniaxial tensile tests using the Allround-Line table-top testing machine (Zwick Roell, Germany). Sample clamping without damage was achieved with a custom-made clamping tool (Fig. S2, ESI†). Tests were prepared by pre-loading the samples with a strain rate of 5 mm min$^{-1}$ until a force of 0.1 N was reached. Subsequently, samples were stretched with a strain rate of 200 mm min$^{-1}$ until rupture. For the calculation of the tensile stress $\sigma$, the measured normal force $F$ was divided by the cross sectional area $A$ of the unstrained sample:

$$\sigma = \frac{F}{A} = \frac{F}{d \cdot b}$$

Here, $b$ is the sample width (4 mm) as defined by the sample geometry (Fig. S1, ESI†) and $d$ is the sample thickness. Because $d$ depends on sample swelling during preparation it was measured for each sample composition with a light microscope.

| Table 1 Minimum (min), maximum (max) and center point (center) parameter values used for investigation of Ca-Alg/PAAm DN hydrogels together with their dimensionless coded values. Coded values are calculated according to eqn (S1) (ESI) so that the minimum parameter values correspond to $-1$ and the maximum parameter values to $1$. |
|---|---|---|---|
| parameter | min | center | max |
| $c_{\text{alg}}$ [wt%] | $0.01$ | $0.02$ | $0.03$ |
| $R_D$ | $0.01$ | $0.02$ | $0.03$ |
| $c_{\text{AAM}}$ [wt%] | $0.01$ | $0.02$ | $0.03$ |
| $c_{\text{MBA}}$ [wt%] | $0.01$ | $0.02$ | $0.03$ |
| Coded values | $-1$ | $0$ | $1$ |
resulting stress–strain curves, the mechanical properties of Young’s modulus $E$, strength $\sigma_{\text{max}}$, toughness $U_T$, and strain at break $\varepsilon_{\text{max}}$ were determined. $E$ was taken as the slope of the initial linear region of the stress–strain curve and was calculated by linear regression. For the regression, the data was first smoothed with a Savitzky–Golay filter\(^{26}\) and as many data points were included until the coefficient of determination $R^2$ dropped to 0.995. The strength $\sigma_{\text{max}}$ was found as the highest occurring stress, while $U_T$ describes the energy absorption of a material during plastic deformation until it fails and was determined by the area underneath the stress–strain curve. The strain at break $\varepsilon_{\text{max}}$ was the maximum reached strain.

### Statistical analysis and model fitting

A full linear model was used to describe each of the experimental responses, for the corresponding expression see eqn (S2) (ESI†). The model contained 11 regression coefficients, i.e., four front factors of the terms proportional to only one parameter ($a_{\text{Alg}}, a_{\text{AAm}}, a_{\text{MBA}}$), six front factors of two parameter interaction terms ($b_{\text{Alg},R}, b_{\text{Alg,AAm}}, b_{\text{Alg,MBA}}, b_{\text{AAm},R}, b_{\text{AAm,MBA}}, b_{\text{MBA},R}$), and one intercept ($T_0$). The statistical evaluation was carried out by analysis of variance (ANOVA) taking into account all 75 independently prepared samples with their coded parameter values. Non-significant model terms with $p > 0.05$ were excluded, except if they were needed to keep the model hierarchical. Experimental data in figures are generally given as mean of the measured values ± standard deviation.

### Results and discussion

#### Experimental plan

Due to the complex composition, a multitude of parameters is relevant for sample preparation and consequently for the properties of Ca-Alg/PAAm DN hydrogels. In order to end up with a manageable experimental plan, we had to select a limited number of parameters which likely influence the results significantly and which could be well controlled (Scheme 1). For this purpose, we compiled an overview of some preparation conditions used in the literature (Table S1, ESI†). From these conditions, together with the mechanical characterization data from the corresponding publications, we concluded that the four parameters Alg concentration $c_{\text{Alg}}$, fraction $R_p$ of high molar mass Alg in total Alg concentration, AAm concentration $c_{\text{AAm}}$, and MBA concentration $c_{\text{MBA}}$ were important parameters for which also no data on two parameter interactions were collected so far.

In order to vary $R_p$, two Alg variants with different molar masses were needed. Therefore, the molar masses of the two Alg variants Protanal LF 10/60 and Manucol LD were investigated by size exclusion chromatography (SEC) (Table 2). Indeed, Protanal LF 10/60 exhibited much larger molar masses than Manucol LD, thus making the two polymers suitable to investigate the effect of the fraction of higher molar mass Alg in the Alg mixture.

#### Tensile tests and resulting stress strain curves

Representative stress strain curves measured for some individual Ca-Alg/PAAm DN hydrogels prepared in this study are shown in Fig. 1. Different shapes of the stress strain curves were observed. Some samples showed a very steep increase of the stress $\sigma$ and subsequent failure at rather low strains $\varepsilon$ (curve 1 in Fig. 1). In other cases, samples could be stretched to very high stresses before failure while still at rather low stresses (curve 6 in Fig. 1). Within the entire dataset, various stress strain curves between these two extremes were measured (curves 3, 4 and 5), with the maximum stress observed in curve 2 (Fig. 1). The stress strain curves could generally be tuned well by adjusting the sample composition, and their general appearance was similar to previous literature reports.\(^{24,25,40}\) In order to further analyze the data, the Young’s modulus $E$, the strength $\sigma_{\text{max}}$, the toughness $U_T$, and the strain at break $\varepsilon_{\text{max}}$ were extracted for all samples and will be discussed in the following section.

Apart from the four varied parameters, all other parameters were fixed. It is conceivable that the unaltered parameters like radical initiator concentration, TEMED concentration, Ca\(^{2+}\) ion concentration and application method, the kind of cross-linking ion (Ca\(^{2+}\) or other metal ions), or sample preparation methodology also have significant effects and are also heavily involved in parameter interactions. However, the envisioned experimental plan with four parameters results in 25 different parameter settings. Due to the general variance observed in tensile tests of hydrogels, we decided to prepare three independent samples for each composition, so that in total 75 samples were investigated. A further increase of investigated parameters would rapidly increase the number of samples, making a realization impractical.

#### Young’s modulus $E$

The measured Young’s modulus $E$ (Table 2) can be submitted to mechanical tests, so that a detailed analysis of the parameter effects and, more importantly, parameter interactions was possible. The tensile tests described in the following section rely on defect-free samples. The main cause for defects were air bubbles entrapped in hydrogel precursor solutions of high viscosity, most relevant for the combination of a high $c_{\text{Alg}}$ and a high $R_p$ and therefore limiting the maximum $c_{\text{Alg}}$ to 5 wt%.

#### Number average molar mass $M_n$

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It has to be noted that for the tensile tests, a secure clamping of the specimens in the testing machine must be achieved. In contrast to previous reports,\(^{24,25}\) we avoided gluing of the hydrogels because we observed optical changes on the glued
dependence of $E$ and Li$_3$Po$_3$. The results for the mechanical properties were repeated even with changes in the thickness of the sample settings (ESI†, Table S3, the order a result of randomization of parameter variations). Additionally, all individual results for the 75 reports and that varying the three parameters (Fig. 2) that the reported range is similar to previous literature reports. Another finding by Li et al. is important to note that Li et al. already varied the ratio of a short chain alginates in the alginate mixture, similar to the variation of $R_P$ in this study. However, they found that there is no big variation of $E$ with the alginate ratio in their experiments, quite in contrast to our findings here where $a_{R_P}$ was 88.6%, indicative of an increase of $E$ with $R_P$. In order to resolve this contradiction, it is useful to look at the significant two parameter interaction terms in Table 3 and 4. Indeed, four of the two parameter interactions were significant, including $b_{Alg,R}$ and $b_{Alg,AAm}$ which is also reflected by the different slopes of $E$ with $c_{Alg}$ depending on the values of $c_{AAm}$ and $R_P$ (Fig. 2(a)). Expressing the experimental parameters from Li et al. in terms of the parameters used in this study, they varied $R_P$ from 0 to 1 with $c_{Alg} = 2.3$ wt%, $c_{AAm} = 16.8$ wt% and $c_{MBA} = 0.01$ wt%. which is rather close to the grey surface plotted in Fig. 2(a). Indeed, at $c_{Alg} = 2.3$ wt%, the slope for $E$ with $R_P$ is quite low, in line with Li et al., thus resolving the contradiction above. It becomes evident that a high $c_{Alg}$ leverages up the effect of $R_P$ on $E$ which has not been recognized in the previous literature studies. Another finding by Li et al. was an $E$ of approx. 1000 kPa by increasing $c_{Alg}$ up to 6.4 wt% while fixing all other parameters. However, our data show that their choice of a rather high $c_{AAm} = 16.8$ wt% was not ideal to maximize $E$: A simultaneous reduction of $c_{AAm}$ when increasing $c_{Alg}$ leads to further increase of $E$ due to the two parameter interaction, especially when at the same time a high $R_P$ is adjusted, which Li et al. also did not do. These results clearly demonstrate that the experimental plan in this study allows one to navigate the entire parameter space more efficiently in order to optimize the responses such as $E$, compared to the univariate approaches followed in the literature so far. Thus, $E$ values between 3.8 kPa and 766.9 kPa were reached.

Looking at the next response, the strength $a_{max}$ generally the trends were similar to the trends observed for $E$ (Fig. 2(b)). Indeed, samples with a high $E$ also had a high $a_{max}$ and vice versa (Figure S3, ESI†). The increase of $a_{max}$ with $c_{Alg}$ is again in line with literature reports. Also the increase of $a_{max}$ with $R_P$ was reported before. Nafici et al. also in principle investigated the effect of $c_{MBA}$ on $a_{max}$, however did not discuss their results accordingly, probably because the effect was very small, if significant at all. The main differences found between $a_{max}$ and $E$ in this study were that for $a_{max}$ $c_{MBA}$ was significant, like...
also the two parameter interaction of $c_{\text{MBA}}$ and $c_{\text{AAm}}$ (Table 3). However, the effect of $c_{\text{MBA}}$, although significant, is not dominating due to the rather small regression coefficients $a_{\text{MBA}}$ and $b_{\text{Alg, MBA}}$. Additionally, $c_{\text{AAm}}$ was not significant, and also did not participate in any parameter interaction. By contrast, like for $E$, the two parameter interaction term $b_{\text{Alg, R}}$ is of great importance due to its relatively large value. Generally, the knowledge about the significant parameters and parameter interactions and the values of the corresponding regression coefficients (Table 4) again allow to fine-tune $\sigma_{\text{max}}$ according to the needs of a specific application in the range between 46.2 kPa and 709.8 kPa. To the best of the authors’ knowledge, this is the highest

![Fig. 2](image-url)
value reported for the tensile strength of Ca-Alg/PAAm DN hydrogels so far, and a direct result of the systematic parameter variation in this study. For example, Li et al. were limited to strengths of approx. 470 kPa although they increased \( c_{\text{Alg}} \) up to 6.4 wt% because they missed using high \( c_{\text{Alg}} \) and \( R_p \) simultaneously.\(^{25} \) Interestingly, the highest strength so far of approx. 550 kPa from Yang et al. was found at rather low \( c_{\text{Alg}} = 1.56 \) wt% and also low \( c_{\text{MBA}} = 0.0076 \) wt% (Table S1, ESI†) which is in contrast to the findings from the present study and other literature.

The third response, the toughness \( U_T \), is shown in Fig. 2(c). We report \( U_T \) as the area under the stress strain curve, like for example also Bakarich et al.\(^{26,27} \) or Du et al.,\(^{45} \) while other literature reports focus on the fracture energy of notched samples.\(^{24,25,41} \) Therefore, only few values are available for direct comparison. Additionally, Bakarich et al. used samples prepared by extrusion-based 3D printing in their tests which usually contain defects, so that generally no consistent trend in \( U_T \) was observed.\(^{26} \) For the analysis of our data, we start again at the experimental center point (all coded parameter values are zero, \( U_T = 726.4 \) kJ m\(^{-3} \)) and think first about univariately changing the parameter values. In this case, only the parameters \( c_{\text{Alg}} \), \( R_p \), and \( c_{\text{AAm}} \) had a significant effect on \( U_T \) while \( c_{\text{MBA}} \) was found to be insignificant (Table 3). The corresponding regression coefficients of the three significant parameters are similar (Table 4), showing a similar effect of the three parameters within the studied parameter space. The toughness range achieved by univariate variation of \( c_{\text{Alg}} \), \( R_p \), and \( c_{\text{AAm}} \) around the center point thus was between 191.5 kJ m\(^{-3} \) and 1346.1 kJ m\(^{-3} \), already covered solely by changing the \( c_{\text{Alg}} \) value. However, like \( E \) and \( \sigma_{\text{max}} \) above, also \( U_T \) is heavily influenced by two parameter interactions with rather high values of the corresponding regression coefficients (Table 3 and 4). Therefore, by multivariate variation of all parameters, a \( U_T \) range between 21.5 kJ m\(^{-3} \) and 2018.0 kJ m\(^{-3} \) is accessible, again demonstrating the advantages of a DoE approach. The reported values are somewhat smaller than the maximum value of 5100 kJ m\(^{-3} \) given by Du et al.\(^{45} \) This can be explained by their very high value of \( c_{\text{AAm}} = 28\% \) (w/v) and also rather high \( c_{\text{MBA}} = 4\% \) (w/v). The importance of the two parameter interactions for \( U_T \) becomes evident when focusing on \( b_{\text{Alg},\text{AAm}} \). At the lowest \( c_{\text{AAm}} \) of 6 wt%, \( U_T \) decreases with increasing \( c_{\text{Alg}} \) (fixing \( R_p = 0.5 \) and \( c_{\text{MBA}} = 0.01 \) wt%) with a slope of \(-88.8 \) kJ m\(^{-3} \) in the coded parameter space, see also the blue surface in Fig. 2(c). Such a trend was also observed by Li et al. for the fracture energy.\(^{25} \) By contrast, at the highest \( c_{\text{AAm}} \) of 19 wt% and again fixing \( R_p = 0.5 \) and \( c_{\text{MBA}} = 0.01 \) wt%, \( U_T \) increases with increasing \( c_{\text{Alg}} \) with a slope of \(398.5 \) kJ m\(^{-3} \).

Interestingly, Sun et al. reported an optimum in fracture energy of approx. 8000 J m\(^{-2} \) for their Ca-Alg/PAAm DN hydrogels.\(^{24} \) This was found by varying the ratio of \( c_{\text{AAm}} \) and total monomer content \( (c_{\text{AAm}} + c_{\text{Alg}}) \). Assuming a correlation between \( U_T \) and the fracture energy, as it is sometimes observed for hydrogels,\(^{51} \) we should also be able to find such an optimum in our data for \( U_T \), which is apparently not present in the data shown in Fig. 2(c). However, when fixing the sum of \( c_{\text{Alg}} \) and \( c_{\text{AAm}} \) to 14 wt%, like done by Sun et al. in their experiments,\(^{24} \) and further using their other parameter settings, we can use our model to calculate a dependency of \( U_T \) against the ratio of \( c_{\text{AAm}} \) and total monomer content (Fig. 3). The result is very similar to the observation from Sun et al., including the apparent optimum in \( U_T \) of 707.6 kJ m\(^{-3} \). However, for our data we can safely say that the thus obtained, apparently optimized result is rather far from the real optimum, and it is conceivable that this is also the case for the parameter settings used to maximize the fracture energy reported by Sun et al.

Futhermore, the unnecessary coupling of the two parameters \( c_{\text{Alg}} \) and \( c_{\text{AAm}} \), results in an awkward path through the parameter space, while pretending a univariate parameter variation, thus concealing the individual parameter influences on \( U_T \).

Finally, the fourth response, the strain at break \( \varepsilon_{\text{max}} \), is plotted in Fig. 2(d). Within the tested sample compositions, a range of \( \varepsilon_{\text{max}} \) between 32\% and 1283\% was observed. When varying multiple parameter values simultaneously, also for \( \varepsilon_{\text{max}} \), two parameter interactions are highly relevant, similar to the other responses. The highest \( \varepsilon_{\text{max}} \) was a result of the combination of low \( c_{\text{Alg}} \), a high \( c_{\text{AAm}} \) and also a low \( c_{\text{MBA}} \). Obviously, a relatively loosely cross-linked PAAm network at a rather high concentration in combination with a low concentration of the Ca-Alg network facilitates a high extensibility of the Ca-Alg/PAAm DN hydrogels. This is also expressed by the corresponding regression coefficients \( (a_{\text{Alg}}, a_{\text{AAm}}, a_{\text{MBA}}, b_{\text{Alg,AAm}}, b_{\text{Alg,MBA}}, b_{\text{AAm,MBA}}) \), all pointing to a larger \( \varepsilon_{\text{max}} \) for the mentioned combination. As a result, the samples with a very high \( \varepsilon_{\text{max}} \) had a very low \( E \) and vice versa (Figure S4, ESI†). The results are in agreement with previous reports although the maximum strain observed is lower than the highest value of 2300\% reported before.\(^{24} \) This can be explained by the differences in the sample preparation procedure. On the one hand, the \( c_{\text{MBA}} \) in the previous report was lower than the minimum value in the present study, on the other hand also the cross-linking density of the Ca-Alg network was presumably lower due to the Alg cross-linking method with CaSO\(_4\) particles.\(^{24} \) Interestingly, our results show only a minor effect of \( R_p \) on \( \varepsilon_{\text{max}} \) quite in contrast to its effect on \( E \), \( \sigma_{\text{max}} \) and \( U_T \). This would generally allow

| Table 4 All regression coefficients resulting from a regression on all responses with equation S2, taking into account the relevant model terms identified by analysis of variance (Table 3) |
|---|---|---|---|---|---|---|---|---|---|---|
| \( r_0 \) | \( a_{\text{Alg}} \) | \( a_R \) | \( a_{\text{AAm}} \) | \( a_{\text{MBA}} \) | \( b_{\text{Alg,R}} \) | \( b_{\text{Alg,AAm}} \) | \( b_{\text{Alg,MBA}} \) | \( b_{R,\text{AAm}} \) | \( b_{R,\text{MBA}} \) | \( b_{\text{AAm,MBA}} \) |
| \( E \) | 207.3 | 172.2 | 88.6 | -67.2 | -10.1 | 81.3 | -45.9 | — | -21.5 | — | 16.7 |
| \( U_T \) | 265.5 | 166.6 | 117.3 | — | 21.7 | 90.6 | — | 36.8 | — | — | — |
| \( \varepsilon_{\text{max}} \) | 726.4 | 281.0 | 204.8 | 242.4 | -46.3 | 243.7 | 126.2 | 135.8 | — | — | -116.5 |
| \( \varepsilon_{\text{max}} \) | 494.8 | -156.5 | -15.1 | 162.8 | -112.9 | -58.5 | 41.9 | 108.4 | — | — | -112.8 |

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Conclusions

Previously the composition of calcium alginate/polyacrylamide double network hydrogels was varied by one parameter at a time approaches. We could show by a design of experiments approach that as a consequence the achieved, already outstanding mechanical properties were most likely not a result of a fully optimized material composition. The regression models presented here agree with literature findings so far, and additionally dramatically extend the knowledge about the Ca-Alg/PAAm DN hydrogel system by analysis of two-factor interactions. The data analysis shows the way to further optimize the parameter settings to reach even more outstanding properties for Ca-Alg/PAAm DN hydrogels. We would also like to encourage future studies on inherently complex hydrogel systems to follow experimental plans like a design of experiments approach in order to be able to identify parameter interaction effects.

Conflicts of interest

There are no conflicts to declare.

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Notes and references

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